

# Adaptive Sampling Using Mobile Robots and a Sensor Network

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## Introduction: Scalar Field Estimation

### Static sensor nodes and mobile robots

- Advantages of static sensor nodes
  - Longer battery life
  - Higher temporal resolution
- Advantages of mobile robots
  - Higher spatial resolution
  - Ability to change the distribution of the readings

### Main idea: Exploit advantages of both

- Static sensors
  - Uniformly deployed across the sensing field
  - Initial estimate generated from the sensor readings
- Mobile robots
  - Additional readings taken in critical locations
  - Estimate refined by using both initial and additional readings

## Problem Description: Coordination between static sensor nodes and mobile robots

### Problem Statement

- Given
  - A set of static sensor nodes uniformly distributed
  - A set of mobile robots
- Goal
  - Coordinate the motion of the mobile robots so that error associated with the reconstruction of the underlying scalar field is minimized

### Assumptions

- Same sensors on mobile robots and static sensors
- Limited energy available to mobile robots
- No change in the scalar field during the data collecting tour
- Local Linear Regression used for estimation
- Centralized processing
- Accurate localization

## Proposed Solution: Combining optimal experimental design and path planning

### Definition of gain

- The Integrated Mean Square Error (IMSE) associated with Local Linear Regression can be estimated as follows:

$$IMSE(X) \propto \int \left( \frac{tr^2\{H_m(\mathbf{x})\}}{n^2 \hat{f}^2(\mathbf{x})} \right)^{\frac{2}{d+4}} dx$$

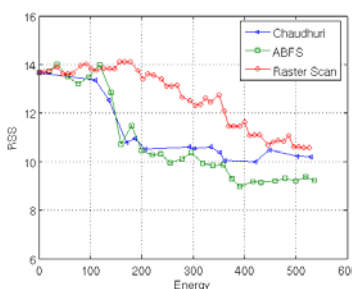
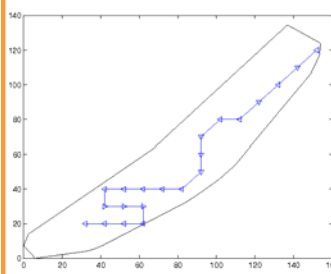
- $H_m(\mathbf{x})$  is the Hessian matrix,  $\hat{f}(\mathbf{x})$  is the estimated local reading density and  $X = \{x_0, x_1, \dots, x_n\}$

- The gain associated with each location  $\mathbf{x}$  is defined as the decrease of the IMSE if more sensor readings taken at  $\mathbf{x}$

$$G(\mathbf{x}) = IMSE(X_0) - IMSE(X_0 \cup \{\mathbf{x}\})$$

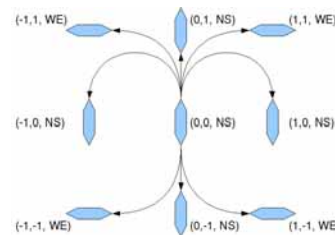
### Path planning for single mobile robot

- Approximate Breadth First Search: Maximizing gain collected with limited initial energy
- K-path: Minimizing the energy consumption while collecting given amount of gain
  - Based on the primal-dual schema
  - Approximation factor  $2+\delta$  for certain gain



### Energy consumption model

- Based on a NAMOS boat
- The boat is assumed to have minimum turning radius
- Energy consumption is proportional to the distance traveled



### Path planning for multiple mobile robots

- Assumptions: All robots have the same initial energy and share the same energy consumption model
- Generate graph representing state transition for single robot
- Partition graph into sub graphs with equal gain
- Assign one mobile robot to each sub graph and apply the path planning for single mobile robots

